

STAT 496
Homework 4 Problems
due Wed. October 26

5 Problems. Show all work.

Please follow the Lab report directions off the homework web page for R Problems. Please work in HW Groups!

Indicate the leader for each problem.

1. Consider the following MA(1) model:

$$Y_t = e_t - 0.6e_{t-1}$$

where $\{e_t\}$ is a mean zero white noise process with constant variance σ_e^2 .

You have already calculated and the ACF for $k = 0, 1, 2, 3, 4, 5$ lags for Homework 3 Problem 2 (a). Now, calculate the PACF ϕ_{kk} by hand for $k = 0, 1, 2$ lags. (You can check your calculations by using the R function `ARMAacf` with the `pacf=TRUE` option.) You do not need to sketch the the PACF. Note: By convention $\phi_{00} = 1$.)

2. p. 172: 7.13.

Use the R `set.seed(1)` for the first simulation and the `set.seed(2)` for the second simulation

- (a) Use the R function `ar`.
- (b) Use the R function `arima` with the method argument `method="CSS"`.
- (c) Use the R function `arima` with the default method argument `method="CSS-ML"`.

3. Repeat Problem 2: p. 172: 7.13, but use a sample size of $n=500$.

4. p. 172: 7.16.

Use the R `set.seed(1)` for the first simulation and the `set.seed(2)` for the second simulation

- (a) Use the R function `ar`.
- (b) Use the R function `arima` with the method argument `method="CSS"`.
- (c) Use the R function `arima` with the default method argument `method="CSS-ML"`.

5. p. 174: 7.26.

- (a) Use the R function `ar`.
 - (b) Use the R function `arima` with the default method argument `method="CSS-ML"`
- In addition, use your fit from (b) and the R `tsdiag` function to make 3 diagnostic plots of the fit. Examine the the first 2 plots. Does it look like the residuals are indeed independent and identically distributed (iid)?